

-- Simplifying Radicals & The Pythagorean Theorem --



Simplifying Radicals

Rules

Examples

- 1) break the number under the square/cube root into factors that can be simplified using the root given (**at least** one of them should be simplifiable)
- 2) determine how many of the numbers you have can be broken down into its square/cube/4th root etc.
- 3) take the square/cube/4th root etc. of all the factorable numbers inside the radical and move it/them outside the radical
- 4) multiply the numbers outside the radical (if necessary)

$$\begin{aligned}\sqrt{18} &\Rightarrow \sqrt{(9 \cdot 2)} \\ \sqrt{9} = 3 &\rightarrow 3\sqrt{2} \\ \sqrt{18} &\approx 4.24; 3\sqrt{2} \approx 4.24\end{aligned}$$

$$\begin{aligned}\sqrt{252} &\Rightarrow \sqrt{(4 \cdot 9 \cdot 7)} \\ \sqrt{4} = 2; \sqrt{9} = 3 & \\ (2 \cdot 3)\sqrt{7} &\Rightarrow 6\sqrt{7} \\ \sqrt{252} &\approx 15.87; 6\sqrt{7} \approx 15.87\end{aligned}$$

$$\begin{aligned}\sqrt[3]{108} &\Rightarrow \sqrt[3]{(27 \cdot 4)} \\ \sqrt[3]{27} = 3 &\rightarrow 3(\sqrt[3]{4}) \\ \sqrt[3]{108} &\approx 4.76; 3(\sqrt[3]{4}) \approx 4.76\end{aligned}$$

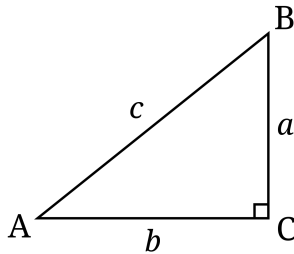
$$\begin{aligned}\sqrt[3]{48} &\Rightarrow \sqrt[3]{(8 \cdot 6)} \\ \sqrt[3]{8} = 2 &\rightarrow 2(\sqrt[3]{6}) \\ \sqrt[3]{48} &\approx 3.63; 2(\sqrt[3]{6}) \approx 3.63\end{aligned}$$

Pythagorean Theorem

Rules

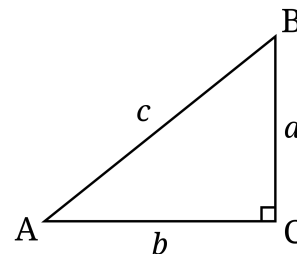
Example

- The Pythagorean Theorem **can only be used on right triangles**



- a right triangle will always have straight vertical and horizontal legs, with a small box at the intersection, indicating a 90° angle
- the formula for the Pythagorean Theorem ($a^2 + b^2 = c^2$) will **ALWAYS** be true for any and all right triangles. "a" and "b" represent the smaller, vertical/horizontal sides ("legs"). "c" represents the diagonal side (hypotenuse). use this formula to find the missing side length
- to use the formula, simply plug in the numbers given, whether "a" and "b", "a" and "c", or "b" and "c". the lengths of the legs added together **MUST BE** larger than the length of the hypotenuse alone
- **Pythagorean Triples** are any 3 numbers that fit the rule for the Pythagorean Theorem. There are some common Pythagorean Triples that you should consider memorizing should you ever encounter them. **Some of these triples include: 3, 4, 5; 5, 12, 13; and 9, 40, 41**

Ex. Suppose in the figure below, "a" is equal to 4 and "b" is equal to 6. Find the length of "c"



$$\begin{aligned}\text{Pythagorean Theorem: } a^2 + b^2 &= c^2 \\ (4)^2 + (6)^2 &= c^2\end{aligned}$$

$$16 + 36 = c^2$$

$$\sqrt{52} = \sqrt{c^2}$$

($\sqrt{c^2}$) will cancel out, leaving just c)

$$c \approx 7.21$$